

## FACULTY OF SCIENCE **Department of Mathematics and Statistics**

## Mathematics 445 /447

### Analysis II / Honours Analysis II

(see Section 3.5C of Faculty of Science www.ucalgary.ca/pubs/calendar/current/sc-3-5.html and Course Descriptions: http://www.ucalgary.ca/pubs/calendar/current/course-main.html)

# Syllabus

Topics	Number of
Sequences of functions; pointwise and uniform convergence; Weierstrass M- test.	hours 6
Topology of metric spaces and normed linear spaces. <i>p</i> -norms on R^n and Minkowski's inequality.	6
Compactness, connectedness, completeness and continuity; the contraction mapping principle; the Baire category theorem.	6
Continuous functions on a compact metric space; approximations of continuous functions: Stone-Weierstrass theorem; the Arzela-Ascoli theorem.	3
Linear transformations and matrix norms.	3
Differentiability on R^n: the Jacobian, the chain rule, the mean value theorem, the inverse function theorem and the implicit function theorem.	8
Additional topics and/or applications selected by course instructor.	4
Total Hours	36

Updated 15 Dec 2016 by R. Hamilton

#### Overview

This course aims to formalize the analogies between the real numbers and other spaces with similar structure. In particular, students will generalize many of the notions in the Analysis I course to more general settings including Euclidean space, spaces of functions and spaces of linear transformations. Honour students in Math 447 are expected to produce a higher level of rigour on written tests and solve more difficult and open-ended assignment problems.

Subject specific knowledge

By the end of this course, students are expected to

- 1. state the axioms of a metric space and deduce conclusions from these axioms.
- 2. show that many of the spaces encountered so far in mathematics are examples of metric spaces.
- 3. construct a formal epsilon argument for the convergence of a sequence in a metric space.
- 4. identify the key topological features of metric spaces and their subspaces.
- 5. verify the completeness of several foundational metric spaces.
- 6. state and prove the Baire category theorem and its equivalents.
- 7. state the axioms of a normed linear space and provide several examples.
- 8. state the contraction mapping theorem, the Arzela-Ascoli theorem, and the Stone- Weierstrass theorem for functions defined on compact metric spaces. Apply these theorems to examples of approximating continuous functions with simpler functions.
- 9. define the notions of differentiability, partial derivatives and the Jacobian matrix for multivariate functions.
- 10. state and apply the implicit function theorem.

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