

AMAT 217 OFFICIAL FORMULA SHEET

A: BASIC INTEGRALS

Let $r, a, \beta \in \mathbb{R}$, $r \neq -1$, $a \neq 0$ and $\beta > 0$.

1. $\int x^r dx = \frac{x^{r+1}}{r+1} + C$
2. $\int \frac{1}{x} dx = \ln|x| + C$
3. $\int e^{ax} dx = \frac{1}{a} e^{ax} + C$
4. $\int \sin(ax) dx = -\frac{1}{a} \cos(ax) + C$
5. $\int \cos(ax) dx = \frac{1}{a} \sin(ax) + C$
6. $\int \tan(ax) dx = \frac{1}{a} \ln|\sec(ax)| + C$
7. $\int \cot(ax) dx = \frac{1}{a} \ln|\sin(ax)| + C$
8. $\int \sec(ax) dx = \frac{1}{a} \ln|\sec(ax) + \tan(ax)| + C$
9. $\int \csc(ax) dx = \frac{1}{a} \ln|\csc(ax) - \cot(ax)| + C$
10. $\int \sec^2(ax) dx = \frac{1}{a} \tan(ax) + C$
11. $\int \csc^2(ax) dx = -\frac{1}{a} \cot(ax) + C$
12. $\int \sec(ax) \tan(ax) dx = \frac{1}{a} \sec(ax) + C$
13. $\int \csc(ax) \cot(ax) dx = -\frac{1}{a} \csc(ax) + C$
14. $\int \frac{1}{\sqrt{\beta^2 - x^2}} dx = \sin^{-1}\left(\frac{x}{\beta}\right) + C$
15. $\int \frac{1}{\sqrt{\beta^2 + x^2}} dx = \sinh^{-1}\left(\frac{x}{\beta}\right) + C$
16. $\int \frac{1}{\sqrt{x^2 - \beta^2}} dx = \cosh^{-1}\left(\frac{x}{\beta}\right) + C$
17. $\int \frac{1}{x^2 + \beta^2} dx = \frac{1}{\beta} \tan^{-1}\left(\frac{x}{\beta}\right) + C$

B: BASIC TRIGONOMETRIC IDENTITIES

GROUP (A):

$$(i) \tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)} \quad (ii) \cot(\theta) = \frac{\cos(\theta)}{\sin(\theta)} \quad (iii) \sec(\theta) = \frac{1}{\cos(\theta)} \quad (iv) \csc(\theta) = \frac{1}{\sin(\theta)}$$

GROUP (B):

$$(i) \cos^2(\theta) + \sin^2(\theta) = 1 \quad (ii) 1 + \tan^2(\theta) = \sec^2(\theta) \quad (iii) \cot^2(\theta) + 1 = \csc^2(\theta)$$

GROUP (C):

$$(i) \sin(2\theta) = 2 \sin(\theta) \cos(\theta) \quad (ii) \cos(2\theta) = 2 \cos^2(\theta) - 1 \quad (iii) \cos(2\theta) = 1 - 2 \sin^2(\theta)$$

GROUP (D):

$$(i) \sin(-\theta) = -\sin(\theta) \quad (ii) \cos(-\theta) = \cos(\theta) \quad (iii) \tan(-\theta) = -\tan(\theta)$$

END