

$$f(x) = ax + b$$

The root is $x = -\frac{b}{a}$.

Case a: If $a > 0$ then when $x < -\frac{b}{a}$, $f(x) < 0$ and when $x > -\frac{b}{a}$, $f(x) > 0$.

x	$-\infty$	$-\frac{b}{a}$	$+\infty$
$f(x)$	-	0	+

Case b: If $a < 0$ then when $x < -\frac{b}{a}$, $f(x) > 0$ and when $x > -\frac{b}{a}$, $f(x) < 0$.

x	$-\infty$	$-\frac{b}{a}$	$+\infty$
$f(x)$	+	0	-

$$f(x) = ax^2 + bx + c$$

Case a: $\Delta = b^2 - 4ac > 0$: two distinct roots exist ($x_1 \neq x_2$):

x	$-\infty$	x_1	x_2	$+\infty$	
$f(x)$	Same as a	0	Opposite of a	0	Same as a

Between the roots $f(x)$ has the opposite sign of a (the leading coefficient) and outside the roots $f(x)$ has the same sign as a .

Case b: $\Delta = 0$: a repeated root (x_1)

x	$-\infty$	x_1	$+\infty$
$f(x)$	Same as a	0	Same as a

$f(x)$ has the same sign as a .

Case c: $\Delta < 0$: no roots

x	$-\infty$	$+\infty$
$f(x)$	Same as a	

$f(x)$ has the same sign as a .

Every polynomial of higher degree can be factorized and written as a multiplication of first and second degree polynomials.