

Practice Problems S7 (Vector Geometry)

- Let $P_1(2, 1, -2)$ and $P_2(1, -2, 0)$ be points in \mathbb{R}^3 .
 - Find the parametric equations of the line through P_1 and P_2 ;
 - Find the coordinates of the point P that is $1/4$ of the way from P_1 to P_2 .

- Find the point of intersection P between the lines (if they are concurrent):

$$\begin{cases} x = 3 + t \\ y = 2 + 3t \\ z = -1 - 3t \end{cases} \quad \text{and} \quad \begin{cases} x = 1 - s \\ y = 1 + 2s \\ z = 3 + s \end{cases} .$$

- Find the equation of the plane passing through the point $P(3, -7, 5)$ and is perpendicular to the line $\begin{cases} x = 2 + 6t \\ y = -5 - 6t \\ z = 3 + 5t \end{cases}$.
- Find the equation of the plane through the points $A(3, -7, 1)$, $B(2, 0, -1)$ and $C(1, 3, 0)$. Check if the point $D(5, 1, 1)$ lies on this plane.

- Determine whether the plane $2x - 3y + z = 1$ contains the line $\begin{cases} x = 3 + 2t \\ y = 2 \\ z = 1 - 4t \end{cases}$.

- Find the line of intersection of the planes $(\pi_1) \equiv 3x + 5y + 4z = 5$ and $(\pi_2) \equiv x + 2y + 3z = 2$.

- Find the shortest distance from the point $P(1, 1, 1)$ to the line $\begin{cases} x = 3 + t \\ y = 9 \\ z = 10 - 4t \end{cases}$.

Which point on this line is closest to P ?

8. Find the shortest distance from the point $P(4, 1, 9)$ to the plane $x - 4z = 2$. Which point on this plane is closest to P ?
9. Find the areas of the sides of the parallelepiped determined by the vectors \overrightarrow{AB} , \overrightarrow{AC} , and \overrightarrow{AD} , where A , B , C and D are the points in Problem 4. What is the volume of this parallelepiped?

Recommended Problems:

Pages 165 - 167: 1 a, c; 3 a; 4 a; 5, 7 a; 9 a, b; 15, 20, 24

Pages 177 - 179: 1 a; 2 a, b; 3 a; 6, 8, 9, 10 a; 11 a; 12, 13, 14, 15, 16 a; 18, 19, 24 a

Page 185: 3 a; 4 a; 5 a.