

NAME _____ ID _____

MATHEMATICS 249

MIDTERM

Fall 2000

SHOW ALL WORK. Marks for each problem are to the left of the problem number.
NO CALCULATORS PLEASE.

[5] 1. Find $\lim_{x \rightarrow 1/2} \left(\frac{5 - 10x}{2x^2 - 7x + 3} \right)$.

[5] 2. Find $\lim_{x \rightarrow 0} \left(\frac{\sin(x^2 - 2x)}{x} \right)$.

[5] 3. Find $\frac{d}{dx} \left(\frac{\tan 2x}{x+8} \right)$.

[5] 4. Find $\frac{d}{dx} \sqrt{\sin x - x \cos x}$.

[5] 5. Find $\frac{d}{dx}((7 - \sec^7 x)^{-7})$.

[5] 6. USE THE DEFINITION OF DERIVATIVE to find $\frac{d}{dx}\sqrt{3 - 5x}$.

[5] 7. An object is moving on a straight line. Its position (distance from a fixed point) at any time t is given by the function $f(t) = 2t^2 - 5t + 2$. Find the instantaneous velocity of the object at time $t = 3$. (Use any method.)

[5] 8. Suppose that $f(x)$ and $g(x)$ are differentiable functions. Use the definition of derivative to prove that $\frac{d}{dx}(f(x) - g(x)) = \frac{d}{dx}f(x) - \frac{d}{dx}g(x)$.