NAME\_\_\_\_\_ID\_\_\_

MATHEMATICS 249

 ${\bf MIDTERM}$ 

Fall 2003

SHOW ALL WORK. Marks for each problem are to the left of the problem number. NO CALCULATORS PLEASE.

[5] 1. Find 
$$\lim_{x \to -1} \left( \frac{\sqrt{1 - 3x} - 2}{x + 1} \right)$$
.

[4] 2. Find 
$$\lim_{x\to 0^+} \left(\frac{\sin 5x}{x\sqrt{x}}\right)$$
.

[5] 3. Find 
$$\frac{dy}{dx}$$
 where  $y = x^3 \cos(1 - 4x)$ .

[5] 4. Find 
$$\frac{d}{dx} \left( \sqrt{4 - \sec(4/x)} \right)$$
.

[5] 5. Find 
$$\frac{d}{dx} \left( \frac{e^{2x}}{x^2 + \ln(x^2)} \right)$$
.

[5] 6. Use implicit differentiation to find  $\frac{dy}{dx}$  where  $x^{3/2} + y^{3/2} = xy + 3$ .

[5] 7. USE THE DEFINITION OF DERIVATIVE to find  $\frac{d}{dx}(3-2x)$ .

[6] 8. Find the equation of the tangent line to the curve  $y = \frac{x^3}{3x^2 - 5}$  at the point on the curve where x = 1.