

The University of Calgary
 Department of Mathematics and Statistics
 MATH 249-01
 Quiz # 1W

Fall 2008

Name: _____ I.D.#: _____

1. Solve for x:

(a) $\frac{8}{x} \geq \frac{x+10}{x+1}$

(b) $|2x+3| > -1$. [4]

2. Find the equation of the line perpendicular to the line $3x - 4y = 4$, passing through the center of the circle $x^2 + y^2 - y = 1$ [3]

3. Simplify and find all x for which the expressions are defined

$$\frac{x-3}{1 + \frac{6x}{x^2+9}} \quad [3]$$

Solution

For 1a)

for $x \neq -1$ $\frac{8}{x} - \frac{10+x}{x+1} \geq 0$ $\frac{8(x+1) - x(10+x)}{x(x+1)} \geq 0$ $\frac{8x+8-10x-x^2}{x(x+1)} \geq 0$
 $\frac{8-2x-x^2}{x(x+1)} \geq 0$ $\frac{x^2+2x-8}{x(x+1)} \leq 0$ $\frac{(x+4)(x-2)}{x(x+1)} \leq 0$ split points $x = 0, -1, -4, 2$

testing $\begin{matrix} pos & & neg & & pos & & neg & & pos \\ x=-5 & - & x=-2 & - & x=-\frac{1}{2} & - & x=1 & - & x=4 \end{matrix}$
 check the split points $x = 0, -1$ No; $x = -4, 2$ O.K.

so $x \in [-4, -1) \cup (0, 2]$

For 1b)

always $|\dots| \geq 0$ so bigger than neg# $(-\infty, +\infty)$ any x

For 2)

the line $3x - 4y = 4$ $y = \frac{3}{4}x - 1$ has the slope $m = \frac{3}{4}$

so the perpendicular line has to have slope $m_{\perp} = -\frac{4}{3}$

to find the center complete the square

$$x^2 + y^2 - 2 \cdot \frac{1}{2}y + \frac{1}{4} = 1 + \frac{1}{4} \quad x^2 + (y - \frac{1}{2})^2 = \frac{5}{4} \quad C(0, \frac{1}{2})$$

and together $y = -\frac{4}{3}x + \frac{1}{2}$.

For 3)

$$\frac{x-3}{1 + \frac{6x}{x^2+9}} = \frac{x-3}{\frac{x^2+9+6x}{x^2+9}} = \frac{x-3}{\frac{(x+3)^2}{x^2+9}} = \frac{(x-3)(x^2+9)}{(x+3)^2} \quad \text{for } x \neq -3 \text{ only.}$$