## The University of Calgary Department of Mathematics and Statistics MATH 249Worksheet #2

1. For 
$$f(x) = \frac{1}{1-x} \left( 1 - \frac{4}{x+3} \right)$$
 find  $\lim f(x)$ 

(a) as 
$$x \to 1$$
 and

(b) as 
$$x \to -3^+$$

(c) as 
$$x \to +\infty$$
.

2. For 
$$f(x) = \sqrt{9 - x^2}$$
 and  $g(x) = \frac{3}{x - 1}$  find the compositions  $g \circ g$  and  $f \circ g$  and their domains.

3. For 
$$g(x) = \frac{4}{2x-8}$$
 and  $f(x) = \sqrt{x^2-9}$  find  $g \circ g$  and  $g \circ f$  and their domains

4. Find: 
$$\lim \frac{1-4x^2}{6x^2-5x+1}$$

(a) as 
$$x \to -\infty$$
 (b) as  $x \to \frac{1}{2}$  (c) as  $x \to \frac{1}{3}$ .

(b) as 
$$x \to \frac{1}{2}$$

(c) as 
$$x \to \frac{1}{3}^-$$
.

5. Find: 
$$\lim \frac{\sqrt{3x} - 3}{\sqrt{2x^2 - 6x}}$$

(a) as 
$$x \to 3^+$$

(a) as 
$$x \to 3^+$$
 (b) as  $x \to +\infty$  (c) as  $x \to 0$ .

(c) as 
$$x \to 0$$
.

6. For 
$$f(x) = \frac{\sqrt{3-x}}{x^2 - 4x + 3}$$
 find  $\lim f(x)$ 

(a) as 
$$x \to 3^-$$
 and

(b) as 
$$x \to 1^+$$

(c) as 
$$x \to +\infty$$
.

7. For 
$$g(x) = \sqrt{3+x}$$
 and  $f(x) = \sqrt{x-5}$  find the compositions  $g \circ g$  and  $f \circ g$  and their domains.

8. For 
$$f(x) = \frac{|x-3| - |x+3|}{x}$$
 find  $\lim_{x \to a} f(x)$ 

(a) as 
$$x \to 0$$
 and

(b) as 
$$x \to -\infty$$

(c) as 
$$x \to +\infty$$
.

9. For 
$$g(x) = \sqrt{3-x}$$
 and  $f(x) = \frac{6}{3x-1}$  find the compositions  $g \circ f$  and  $f \circ f$  and their domains