MATHEMATICS 251

Practice #2

1. Find the following limits

(a)

$$\lim_{t \to 0} \frac{t-3}{t^3-27}$$
(b)

$$\lim_{s \to -1} \frac{s^2+3s+2}{s^2-s-2}$$
(c)

$$\lim_{z \to 0} \frac{x^2-x}{x^2+x}$$

2. Let f(x) be defined by

$$f(x) = \begin{cases} |x| - 1 & x > -1\\ \sin \pi x & x < -1 \end{cases}$$

Can f be defined at x = -1 so that f is continuous on the whole real line?

3. If

$$f(x) = x^5 + \frac{x^2}{x^2 + 1}$$

show that there is a number ξ such that $f(\xi) = 0$.

- 4. Find the line tangent to the graph of $y = 3 4x^2$ at the point (2, -13).
- 5. Use the *definition* of the derivative to compute f'(9) if $f(x) = \sqrt{x}$.
- 6. Prove that if f is differentiable at x = a, and $f(a) \neq 0$, then

$$\left(\frac{1}{f}\right)'(a) = \frac{-f'(a)}{(f(a))^2}$$

7. Find the equation(s) of all lines tangent to the parabola $y = (x-1)^2+2$ that also pass through the origin.

8. Find
$$f'(3)$$
 if $f(x) = \sqrt{1 + \sqrt{1 + \sqrt{1 + x}}}$.

9. Find r'(3) if

$$r(x) = \frac{(x-1)(x+2)}{(x+1)(x-2)}.$$