

The University of Calgary  
Department of Mathematics and Statistics  
MATH 349 -01/02  
Quiz # 2R

Fall,2007

Name: \_\_\_\_\_ I.D.#: \_\_\_\_\_

1. Find the sum of the series  $\sum_{n=1}^{\infty} \frac{(-1)^n \pi^{n+2}}{4^{2n}} = \pi^2 \sum_{n=1}^{\infty} \left(\frac{-\pi}{16}\right)^n = \pi^2 \cdot \frac{\left(\frac{-\pi}{16}\right)}{1 + \frac{\pi}{16}} = \frac{-\pi^3}{16 + \pi}$   
using  $\sum_{n=N}^{\infty} r^n = \frac{r^N}{1-r}$  for  $-1 < r < 1$ .

2. Is the series  $\sum_{n=2}^{\infty} \frac{1}{n\sqrt{\ln n}}$ .convergent or divergent?Explain.

By Integral Test::  $f(x) = \frac{1}{x\sqrt{\ln x}}$  is cont. positive and decr ( $=\frac{1}{incr}$ ) for  $x \geq 2$

$$\int_2^{\infty} \frac{dx}{x\sqrt{\ln x}} = \left( \text{subst. } u = \ln x, du = \frac{dx}{x} \right) = \int_{\ln 2}^{\infty} \frac{du}{\sqrt{\ln u}} = \left[ 2\sqrt{\ln u} \right]_{\ln 2}^{\infty} = \infty$$

the integral is divergent so is the series.

3. Is the series  $\sum_{n=2}^{\infty} \cos\left(\frac{1}{n}\right)$ .convergent or divergent?Explain.

The series is divergent. since  $\lim_{n \rightarrow \infty} \cos \frac{1}{n} = \cos 0 = 1 \neq 0$  necessary condition