

THE UNIVERSITY OF CALGARY
DEPARTMENT OF MATHEMATICS & STATISTICS
MATHEMATICS 353-02
QUIZ #1T

WINTER 2006

NAME: _____ **I.D. No.:** _____

1. Find ∂S - boundary of S . Is S closed? Open? Bounded? **Sketch** the set.

(a) $S = (x, y) \mid \frac{x}{|y|} \leq 1\}$

(b) $S = \{(x, y, z) \mid 2x^2 + 3y^2 + z^2 \leq 1, z \geq 0\}$ [5]

2. Find all local extrema of $f(x, y) = ye^{x^2-2y^2}$ in its domain. Explain. [5]

SOLUTION

for 1a)

it must $y \neq 0$ so the x -axis is out

since $|y| > 0$ we can multiply and $x \leq |y|$

so all points above or on $y = x, y > 0$ are in

and for $y < 0$ $x \leq -y, -x \geq y$ below and on the line

the set UNBDD

and the boundary is $\partial D = \{y = \pm x, x > 0\} \cup \{y = 0, x \leq 0\}$

first part is included, the second excluded so **neither open nor closed.**

for b)

$2x^2 + 3y^2 + z^2 = 1$ is an ellipsoid, $z \geq 0$, means top half

the set is all points inside or on and above tr on the xy-plane

therefore the set BDD, and the boundary consists of two parts

bottom and shell

$$\partial S = \{2x^2 + 3y^2 \leq 1, z = 0\} \cup \{2x^2 + 3y^2 + z^2 = 1, z \geq 0\}$$

both are included so the set is **closed.**

For 2)

f is defined, continuous, differentiable everywhere, for critical points solve

$$f_x = 2xye^{x^2-2y^2} = 0 \quad \text{so } x = 0 \text{ or } y = 0$$

$$f_y = e^{x^2-2y^2} (1 - 4y^2) = 0 \quad \text{so } y = \pm \frac{1}{2}$$

we got 2 critical points $(0, \frac{1}{2}), (0, -\frac{1}{2})$

for Second Derivative Test

$$f_{xx} = 2ye^{x^2-2y^2} (1 + 2x^2) \quad f_{xy} = 2xe^{x^2-2y^2} (1 - 4y^2) \quad f_{yy} = e^{x^2-2y^2} (-12y + 16y^3)$$

Now

points	A	B	C	D	
$(0, \frac{1}{2})$	$e^{-\frac{1}{2}}$	0	$-4e^{-\frac{1}{2}}$	pos	saddle
$(0, -\frac{1}{2})$	$-e^{-\frac{1}{2}}$	0	$4e^{-\frac{1}{2}}$	pos	saddle

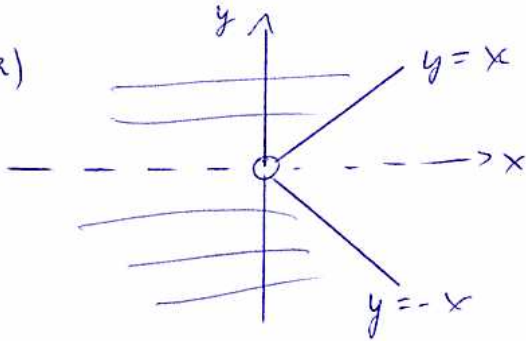
where $D = B^2 - AC$

Quiz #1

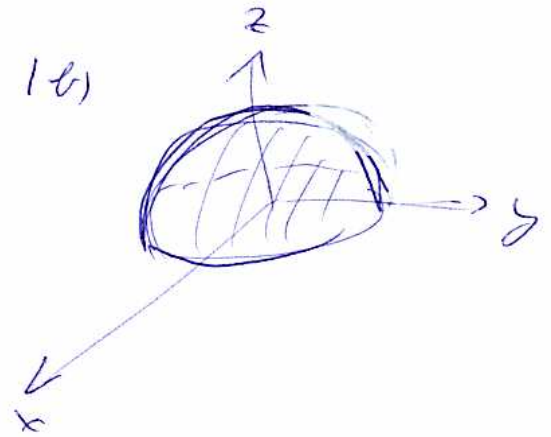
T 04

Tue 10 am

1 a)



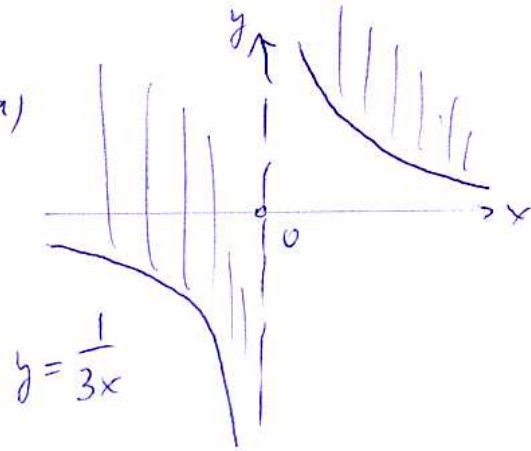
1 b)



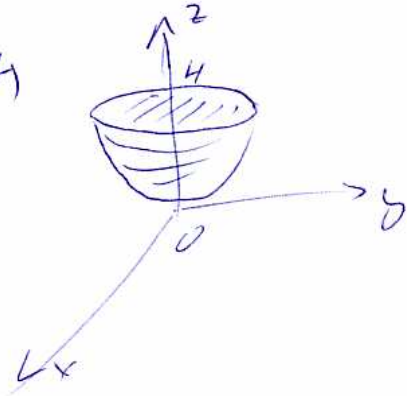
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Tue 3 pm

1 a)



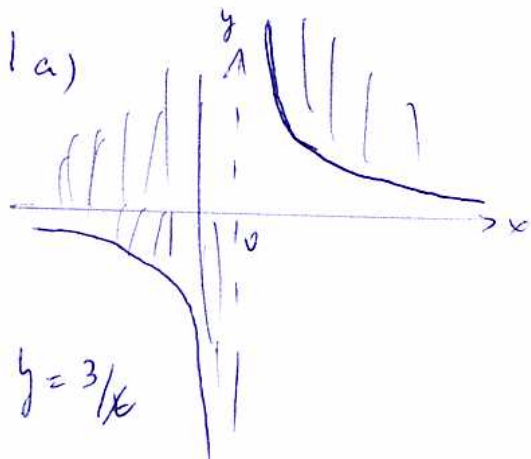
1 b)



T 01 + 02

Tue 2 pm

1 a)



1 b)

