

**The University of Calgary**  
**Department of Mathematics and Statistics**  
**MATH 353      Handout #4**

1. Given  $\mathbf{F}(x, y, z) = (3x^2yz, kyz + x^3z, x^3y + 1 + y^2)$ .
  - (a) Find the value of  $k$  so that the field  $\mathbf{F}$  is conservative.
  - (b) Then, find a potential of  $\mathbf{F}$ .
2. Evaluate  $\int_c f \, ds$  where  $f(x, y, z) = z^2$  and  $c$  is the part of the line of intersection of two planes  $x + y - z = 1$  and  $2x + y - 3z = 0$  between the  $xy$ -plane and the point  $D(3, 0, 2)$ .
3. For  $\mathbf{F}(x, y) = (ky^2 + x, xy - \frac{1}{\sqrt{y}})$  find the value for  $k$  so that the field is conservative, then find a potential.
4. Evaluate  $\int_c z \, ds$  and  $c$  is the intersection of the plane  $z - y = 1$  and the vertical surface  $0 = x - y^2$  between  $A(1, -1, 0)$  and  $B(0, 0, 1)$ .
5. Find  $\int_c \mathbf{F} \cdot d\mathbf{s}$  where  $\mathbf{F}(x, y, z) = (z, e^{\frac{y}{x}}, 2x)$  is given by  $\mathbf{r}(t) = (t, t^2, e^t)$ ,  $t \in [1, 2]$ .
6. For  $\mathbf{F}(x, y) = (3x\sqrt{x^2 + y^4} + \cos x, ky^3\sqrt{x^2 + y^4} + \sin y)$  find the value for  $k$  so that the field is conservative, then find a potential.
7. Evaluate  $\int_c z \, ds$  and  $c$  is given by  $\mathbf{r}(t) = (t \cos t, t \sin t, t)$ ,  $t \in [0, 1]$ .
8. Find  $\int_c \mathbf{F} \cdot d\mathbf{s}$  where  $\mathbf{F}(x, y, z) = (y, z, 2x - z)$  and  $c$  is the intersection of the plane  $z = 2x$  and the paraboloid  $z = x^2 + y^2$  oriented counter-clockwise.