

MATH 353
Handout #5

1. Find the surface area of the part of the sphere $x^2 + y^2 + z^2 = 2$ that lies inside the paraboloid $z = x^2 + y^2$.
2. Find the flux of $\mathbf{F} = \mathbf{i} + \mathbf{j} + z(x^2 + y^2)^2\mathbf{k}$ out of the surface (including top and bottom)
 $S = \{(x, y, z); x^2 + y^2 = 4, 0 \leq z \leq 3\}$.
3. Find the surface area of S
 - (a) which is the part of the cylinder $x^2 + y^2 = 4$ in the first octant below the plane $2x + y + z = 5$;
 - (b) which is the part of the plane $2x + y + z = 5$ inside the cylinder $x^2 + y^2 = 4$.
4. Find the flux $\int \int_S \mathbf{F} \cdot d\mathbf{S}$ where S is the part of the cylinder $y^2 + z^2 = 4$ which lies inside the cylinder $x^2 + y^2 = 4$, above the xy -plane, oriented upward,
and the field is $\mathbf{F}(x, y, z) = (x^2yz, y, xz)$.
5. Evaluate $\int \int_S zx \, dS$ where S is the part of $z = \frac{x^2}{2}$ which lies inside $x^2 + y^2 = 1, x > 0, y < 0$.
6. Evaluate $\int \int_S x^2 dS$ where S is the part of the plane $x + y + z = 2$ inside the cylinder $x^2 + 2y^2 = 1$.