

PMAT 315
ASSIGNMENTS WINTER 2010

Assignment 1.

1. §1.1, #15. Prove the well-ordering axiom by strong induction. [**Hint:** If X is a nonempty set of non-negative integers with no smallest member, let p_n be the statement $n \notin X$.] 7 marks
 2. §1.2, #14. Show that $\gcd(m+n, m) = \gcd(m, n)$. 7 marks
 3. §1.2, #17. If $\gcd(m, n) = 1$ and $\gcd(k, n) = 1$, show that $\gcd(mk, n) = 1$. 6 marks
 4. §1.3, #22(c). In \mathbb{Z}_{20} find the inverse of $\overline{11}$ and use it to solve $\overline{11}x = \overline{16}$. 6 marks
 5. §1.3, #29(b). Show that \bar{a} is invertible in \mathbb{Z}_n if and only if $\bar{a}\bar{b} = \bar{0}$ implies $\bar{b} = \bar{0}$. 7 marks
 6. §1.4, #26. Let γ be any cycle of length r . If $\sigma \in S_n$, show that $\sigma\gamma\sigma^{-1}$ is also a cycle of length r .
More precisely, if $\gamma = (k_1 k_2 \cdots k_r)$ show that $\sigma\gamma\sigma^{-1} = (\sigma k_1 \sigma k_2 \cdots \sigma k_r)$. 7 marks
- Total 40 marks