

PMAT 503.01

Elliptic Curves and Cryptography

**Calendar Description:** An introduction to elliptic curves over the rationals and finite fields. The focus is on both theoretical and computational aspects; subjects covered will include the study of endomorphism rings, Weil pairing, torsion points, group structure, and effective implementation of point addition. Applications to cryptography will be discussed, including elliptic curve-based Diffie-Hellman key exchange, El Gamal encryption, and digital signatures, as well as the associated computational problems on which their security is based.

**Prerequisites:** PMAT 315 Abstract Algebra (or consent of instructor)

**Recommended Preparation:** PMAT 418 Introduction to Cryptography

**Assessment:**

40% assignments

60% research project (proposal, written report, presentation)

**Notes:** This course will share lectures with PMAT 629. Students will be assessed in a similar way, but with reduced expectations as compared to the graduate students. In particular, students will complete roughly 75% of the assignment questions, and the research projects will be less ambitious, with topics assigned by the instructor.

(see Course Descriptions under the year applicable: <http://www.ucalgary.ca/pubs/calendar/> )

## Syllabus

<u>Topics</u>	<u>Number of hours</u>
<b>Finite Fields:</b> overview, extension fields, construction	3
<b>Introduction to Elliptic Curves:</b> Weierstrass equation, group law, projective space and points at infinity, elliptic curves in different characteristics, other models	7
<b>Elliptic curve cryptography:</b> elliptic curve based Diffie-Hellman, ElGamal, and digital signature algorithm	3
<b>More on elliptic curves:</b> endomorphism ring, singular curves, supersingular curves	4
<b>Torsion groups:</b>	3

torsion points, Weil pairing, group structure

**Elliptic curves over finite fields:**

6

Frobenius endomorphism, subfield curves, reduction, order, Hasse-Weil bound

**Security of elliptic curve cryptosystems:**

3

discrete logarithm problem, Weil descent, Weil and Tate pairing, other weak curves

**Efficient implementation:**

3

field representations, bases, group law, exponentiation

**TOTAL HOURS** 

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 **32**

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Date: Dec. 6, 2013  
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