PMAT 613 L01 Fall 2009 Assignment 2

Questions taken from the text by I. Stewart (3rd Edition) will be specified by page and number. Due Oct 9, 2009.

- 1. Show that the Gaussian integers $\mathbb{Z}(i)$ are a euclidean domain, where $\partial(a+bi)=a^2+b^2$.
- 2. Show that $\mathbb{Z}(\omega)$ is a euclidean domain, where $\partial(a+b\omega)=a^2-ab+b^2$. [Hint: this is actually closely related to Question 1.]
- 3. In a euclidean domain (D, ∂) , show that q, r are unique in the division algorithm.
- 4. 3.1a, 3.1b
- 5. 3.2a, 3.2b
- 6. 3.3a, 3.3b
- 7. 3.4
- 8. 3.5
- 9. 3.6 for 3.5b