



Statistics 421

Mathematical Statistics

Multivariate Normal distribution. Limit distributions. Sufficient statistics. Completeness of families of distributions. Exponential families. Likelihood ratio tests. Chi-square tests. Analysis of variance. Sequential tests. Introduction to nonparametric methods, Bayesian theory, the general linear model.

Course Hours: H(3-0)

Prerequisite(s): [Mathematics 323](#) and [353](#).

Suggested Texts:

1. Hogg & Craig, Introduction to mathematical statistics
2. Casella & Berger, Statistical Inference

Syllabus

Topics

**Number
of Hours**

Review – Handouts with examples, review problems on: common univariate distributions; use of cdf, mgf, pdf; variable transformations (Jacobians, graphical domain transformation); distribution of order statistics.

2

Multivariate Normal Distribution

definition, mgf, joint marginals, constant density contours; distributions of linear combinations of MVN random variables.

3

Limit Distributions

concept of a degenerate distribution; convergence in distribution (use of the cdf, mgf); convergence in probability; proof of the CLT; use/proof of Slutsky's theorem.

5

Sufficiency and Completeness

concept of a sufficient set of statistics, factorization theorem; Rao-Blackwell theorem; concept of a complete family of distributions; completeness and uniqueness (Lehmann-Scheffe theorem); minimal sufficient and ancillary statistics; completeness and independence (Basu's theorem); minimum variance unbiased estimation; Cramer-Rao inequality.

8

Exponential family of distributions

2

LR Tests

review of likelihood ratio, Neyman-Pearson lemma; power of a test, uniformly most powerful test; noncentral t, chi-square, F distributions.

5

Normal Models

Cochran's theorem on quadratic forms (no proof); chi-square tests; analysis of variance.

5

Additional Topics - Selections from the following topics should constitute about 6-8 hours.

6

- sequential tests
- general linear model
- nonparametric tests (sign, Wilcoxon)
- Bayesian theory

TOTAL

36
