



UNIVERSITY OF CALGARY
FACULTY OF ARTS
Department of Philosophy

Phil 379 Lec 01
Logic II
Winter 2022
MW 14-15:15 SA 147

December 20, 2021

1 Who's teaching this?

Instructor: Gillman Payette (he/him)
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Office Hours: by appointment (not on the weekend)

Teaching Assistants: [Alexandra Cunningham](#) (she/her)
Email: alexandra.cunningham@ucalgary.ca
Office Hours: by appointment (not on the weekend)

2 How do I get in touch with you?

1. Your question may already be answered on the course discussion board (or in this outline). Check there first. If it is not, consider posting your question in the discussion board instead of sending an email. Instructor and TA will monitor the discussion boards and attend to questions regularly.
2. If your inquiry is specific to your personal situation, feel free to send an email.
3. Ensure that "Phil 279" occurs in the subject line of your emails about this course. Otherwise there is a strong possibility that your message will be deleted unread as spam.
4. Please make sure your first and last names are clearly included in the body of any email message.
5. If you want to make an appointment please indicate the times when you are available.
6. We will do our best to reply within one business day. Please don't expect responses outside business hours.
7. It is customary to address university instructors by their title ("Dr. Payette" or "Prof. Payette") but I won't be offended if you call me 'Gillman'. Please don't call me 'Mr. Payette' or 'Sir'.

3 What is this course about?

Formal logic has many applications both within philosophy and outside (especially in mathematics, computer science, and linguistics). This second course will introduce you to the concepts, results, and methods of formal logic necessary to understand and appreciate these applications as well as the limitations of formal logic. It will be mathematical in that you will be required to master abstract formal concepts and to prove theorems *about* logic (not just *in* logic the way you did in Phil 279); but it does not presuppose any (advanced) knowledge of mathematics. We will start from the basics.

We will begin by studying some basic formal concepts: sets, relations, and functions, and the sizes of infinite sets. We will then consider the language, semantics, and proof theory of first-order logic (FOL), and ways in which we can use first-order logic to formalize facts and reasoning about some domains of interest to philosophers, computer scientists, and logicians.

In the second part of the course, we will begin to investigate the meta-theory of first-order logic. We will concentrate on a few central results: the completeness theorem, which relates the proof theory and semantics of first-order logic, and the compactness theorem and Löwenheim-Skolem theorems, which concern the existence and size of first-order structures.

In the third part of the course, we will discuss a particular way of making precise what it means for a function to be computable. To this end, we will discuss a “model of computation”: Turing machines. We will show that there are problems which are *undecidable* in the sense that there is no Turing machine which, in a finite amount of time, provides a definite yes-or-no answer. The first example of an undecidable problem is the *halting problem*, i.e., the problem of deciding, given the description of a Turing machine, whether it halts on a given input. We will also show that the *decision problem*—i.e., the problem of deciding, given a sentence of first-order logic, whether it is valid—is undecidable.

If there is time, we will cover some advanced topics at the end of the semester, such as second-order logic or solvable cases of the decision problem.

This is a course in *metalogic*. It builds upon the material in Logic I (Phil 279/377), but is very different in character. Doing well in Phil 279 is no guarantee that this will come easy to you.

4 How will the course be run?

The course will be delivered in a **hybrid in-person/online** model. There will be readings, prerecorded lecture videos, discussion boards, and quizzes/tests on the course website (D2L). The passive content, i.e., me explaining things and working through examples, will mostly be delivered asynchronously (that means: not at a specific time). You can read, watch, and participate in discussions more or less when you choose. There will also be in-person sessions on Wednesday which will be run like tutorials where everyone can participate at the same time:

What?	When?	Where?	Who?
“Lecture”	W 14–15:15	SA 147	Instructor & TA

Each “lecture” is meant to be mostly active learning time and will be organized as follows. The first 30 min. (approx.) will deal with questions regarding material from the recorded lectures. Then there will be 45 min. of exercises based on that material.

5 What prerequisites do I need for this course?

Phil 279 Logic I. All of the material from that course will be assumed as common knowledge for this course.

6 What will I learn in this course?

By the end of the course, you should be able to ...

1. Understand, construct, and formulate simple mathematical proofs in which you apply definitions, identify hypotheses, and correctly and appropriately use informal patterns of mathematical reasoning.
2. Understand and apply the methods of definition by induction and proof by induction, both for the natural numbers and for inductively defined sets such as the set of formulas of first-order logic.
3. Understand and use the vernacular of set theory (sets, relations, functions) to describe and explain the metalogical properties of the model and proof theory of first-order logic as well as of Turing machines and computable functions, and to prove intermediate facts about infinite sets and their sizes using, e.g., the diagonal method of Cantor’s theorem.
4. Understand the formal syntax, model theory, and proof theory of first-order logic, to explain the definitions, the properties, and the relationships between logical notions (free and bound variables, sentences, satisfaction, consequence and satisfiability, inference rule, derivation, provability and consistency), and to prove intermediate facts about them (such as the soundness of the proof system).

5. Understand the completeness theorem of first-order logic, to explain the overall structure as well as the individual steps of the proof, to explain and prove from it corollaries such as the compactness and Löwenheim-Skolem theorems, and to apply these to properties of theories and the size of models thereof.
6. Understand the concept of Turing machines, how they can be used to define computable functions, to construct simple Turing machines, to formulate and prove the undecidability of the halting problem, and to formulate and explain the decision problem.

7 What will I have to do in this course?

7.1 Visit the D2L/Brightspace site

The course has a [D2L/Brightspace](#) site. You will find (information on) course readings, videos, assignments, quizzes, tests, and grades there. Any updates, including revisions to the course schedule, PASS sessions, course schedule, will be posted there. **To make sure you don't miss a deadline or an important update, please review your [notification settings](#).**

7.2 Read the textbook

The textbook is:

Sets, Logic, Computation: An Open Introduction to Metalogic (Fall 2021 edition)

It is free and available on D2L in PDF. You may also purchase a paper copy if you like.

You should read along as we cover the topics in the course. Each unit in the Content section on D2L will tell you which chapters of the book to read. We won't cover, and you won't be tested on, everything in the book.

7.3 Watch some lecture videos

Each week, there will be lecture videos. You should watch these videos in preparation for the in-person class meetings, i.e., before Wednesday. The videos are posted on D2L, as are the slide decks that go with them.

7.4 Attend in-person sessions

We'll have in-person sessions every week on Wednesdays, 14:00–15:15. During these meetings, we will work on problems related to the week's material, often in small groups. I'll assume that you're prepared (i.e., have watched the lecture videos and done the reading). There will also be opportunity for Q&A and discussion.

7.5 Ask and answer questions on the discussion board

There will be a discussion board for the course set up on CampusWire. You might want clarification on something in lecture or the textbook, or you're stuck on an exercise and need a hint or have someone to tell you what the problem with your proposed solution is. Your instructor and TAs will help. One of the course outcomes, however, is to make you a better, more collaborative learner and teacher yourself. So feel free to attempt to explain things others ask questions about, and provide hints for those who get stuck yourself.

Pre-class quizzes

There will be 10 open-book pre-class quizzes covering the background readings, to be taken online on D2L. Quizzes will be due at 14:00 of the first day the relevant topic is discussed in class, but will be available on D2L for seven days prior. Pre-class quizzes are graded either complete or not complete.

Weekly tests

There will be 10 open-book tests covering the topics in class, to be taken on D2L. Tests are graded pass/no pass. Look for the due dates for these tests on D2L.

Proof Problems

There will be 10 proof-like problems. They will usually be due on Mondays at 23:59, to be submitted on D2L or Carnap. The first problem will be due. Basic problems are graded according to the EMRN rubric below. If you score R you will be able to resubmit the problem.

Group work

Some of the class time will be devoted to working on sample problems. You are expected to do the assigned readings before coming to class and the pre-class quizzes are meant to ensure some understanding of the material. At irregular intervals we will solve problems in small groups. A certain level of participation is expected and is reflected in the assessment scheme. You must participate in a certain number of classes for each grade letter. You can make up **some** of the class participation by commenting on problems posted on CampusWire.

8 What do I need for all that?

This course will be delivered partly online; lectures are posted online. To access the material and complete the assignments you will need a computer and access to the internet (for some things a smartphone or tablet are enough, but a desktop or laptop with a keyboard, mouse, and large-ish screen will be much more comfortable).

You will need an account with the UCalgary IT service, without which you cannot access D2L.

Instructions for getting IT and Zoom accounts, accessing D2L, and additional tips for how to best learn online are available at:

taylorinstitute.ucalgary.ca/learning-continuity

9 How will my grade be determined?

There will be no registrar-scheduled final exam.

Your work is evaluated on one of three scales, depending on what it is:

1. Pre-class quizzes and in-class group work are graded either **credit (CR)** or **no credit**. To get credit, you must score at least 50% on a quiz, or participate in the group work exercise in a given week.
2. Weekly tests are graded either **pass (P)** or **no pass**. To count as a pass, you must get a point score of at least 70%.
3. Proof Problems are graded using the four-level EMRN rubric, illustrated below. Marks of **E** (exemplary) and **M** (meets expectations) are “passing”. Marks of **R** (needs revision) and **N** (not assessable) are not passing.

Please note that with the exception of the weekly tests, none of the work in the class is assessed using points. **Your progress toward a grade in the course is determined simply by the quantity of passing marks you earn on various assignments and how many E marks you receive on problems.** This is a “competency based” approach to grading that gives you full control over how you earn your grade and provides transparency as to what you have shown competence and what you still need to work on.

EMRN rubric

- If your work demonstrates thorough understanding of the concepts and meets the expectations outlined in the assignment. . .
 - and the work is complete and well documented, it earns an **Exemplary (E)** mark.
(The work meets or exceeds the expectations of the assignment. Communication is clear and complete. Mastery of concepts is evident. There are no nontrivial errors. This work could be used as a classroom example.)
 - otherwise, it earns a **Meets Expectations (M)** mark.
(Understanding of the concepts is evident through correct work and clear explanations. Some revision or expansion is needed, but no significant gaps or errors are present. No additional instruction on the concepts is needed.)

- if not, but . . .
 - there is evidence of partial understanding, it earns a **Revisions Needed (R)** mark.
(Partial understanding of the concepts is evident, but significant gaps remain. Needs further work, more review, and/or improved explanations.)
 - otherwise, it earns a **Not Assessable (N)** mark.
(Not enough evidence is present in the work to determine whether there is understanding of the concepts. The work is fragmentary, contains significant errors or omissions, or there are too many issues to justify correcting each one.)

Course grade

To receive a Credit grade in the class, you must:

- earn a passing grade on at least 6 problems;
- earn at least 1 E grade;
- pass at least 8 tests.

The table below shows the minimum requirements in order to earn a particular letter grade in the course.

Grade	Q	T	PP		GW
	(CR)	(P)	(\geq M)	(E)	
A+	10	10	10	8	8
A	10	10	10	8	6
A–	10	10	9	5	6
B+	10	9	8	3	6
B	8	9	8	2	5
B–	8	9	8		5
C+	7	8	7		5
C	7	8	7		4
C–	7	7	6		4
D+	7	6	6		4
D	6	6	6		

For instance, to receive a B+ in the course, you must get credit on at least 10 quizzes, pass 9 tests, receive an M or better, of which 3 must be an E, on at least 8 proof problems, and participate in at least 6 “classes”.

Revision

You have the opportunity to revise almost any item of work in the class if you want to raise your grade on it. Specifically:

1. You can retry weekly tests up to 3 times, until the deadline.
2. You can resubmit any basic or challenge problem on which you received a grade of at least R once, up to seven calendar days after the graded problem was returned.
3. You can use a token (see below) to revise any basic or challenge problem on which you received a grade of N.

Tokens

Tokens are a kind of currency for this class. Each student has five (5) tokens to spend to bend the rules of the class in various ways. You can use a token to do the following.

1. Revising a problem on which you received an N grade (see above).
2. Submitting a problem by the deadline for revisions if you did not turn it in.
3. Purchase a no-questions-asked extension of 48 hours on any problem.
4. Purchase a single attempt on a weekly test after the deadline has passed.

10 Are there PASS sessions for this course?

Maybe.

11 What course policies should I be aware of?

11.1 Conduct

Learning can only happen well if everyone feels like they belong and are free to ask questions and participate in discussions. It is partly on you to make sure our course is such a space. So please be respectful, positive, and constructive in your participation in the course. It should go without saying, but do not post (links to) anything racist, misogynist, or homophobic, or NSFW, and don't stalk or harass your fellow students or instructors. Also, do not share links or passwords to live or recorded Zoom sessions outside the course.

11.2 Late policy

If you do not complete an assignment by its deadline, it counts as not completed and will not be assigned a mark. However (see above) you can spend tokens to extend a deadline by 48 hours, or to complete an assignment after the deadline.

If there are factors beyond your control, and which you could not reasonably have planned for, which prevent you from completing activities (illness, family emergency, etc.) please contact the instructor so we can make arrangements. Please do so **as soon as possible**. You will not have the opportunity to make up work you missed early in the term if you don't tell me until the last week of term.

11.3 Plagiarism

You might think that it's only plagiarism if you copy a term paper off the internet. However, you can also plagiarize in a logic course, e.g., by copying a proof verbatim from the textbook or the internet (and only making the necessary changes to apply it to the assigned problem.) The point of logic problems which are similar to the proofs in the text is to make you work through those proofs, understand them, and then prove a similar result on the problem sets. Hence, all solutions must be in your own words; copying or paraphrasing closely from the text or elsewhere constitutes plagiarism, which must be reported to the Dean's office by university policy. It may result in a failing grade or worse penalties.

11.4 Checking your grades and reappraisals of work

University policies for reappraisal of term work and final grades apply (see the *Calendar* section "[Reappraisal of Graded Term Work](#)"). In particular, term work will only be reappraised within 10 calendar days of the date you are advised of your marks. Please keep track of your assignments and your marks (check them on D2L).

12 When is it all going down?

Due dates are tentative and subject to revision. Quizzes are due Wednesdays at 14:00 each week and are on the material covered that week. Tests and proof problems are due Mondays at 23:59 and typically are on the material covered the preceding week or two.

Week	Topics and readings (chapters)		Q	T	PP
1	Jan 10	Introduction			
1	Jan 12	Sets and proofs (1, A)	1		
2	Jan 19	Relations, functions, proofs by induction (2, 3, B)	2	1	
3	Jan 26	Countable and uncountable sets (4)	3	2	1
4	Feb 2	Syntax of FOL (5, 6)	4	3	2
5	Feb 9	Semantics of FOL (7)	5		3
6	Feb 16	Theories and models (8)	6	4	4
		Feb 20–26: Term Break			
7	March 2	Sequent Calculus (9, 10)	7	5	5
8	March 9	Completeness (12)	8	6	6
9	March 16	Consequences of completeness (12)		7	7
10	March 23	Turing machines (14)	9	8	8
11	March 30	The halting problem, reductions (15)	10	9	9
12	April 6	The decision problem (15)			10
13	April 11	Additional topics		10	

13 Important departmental, faculty, and university information

13.1 Academic accommodations

It is the student's responsibility to request academic accommodations according to the University policies and procedures. The student accommodation policy can be found at: www.ucalgary.ca/legal-services/sites/default/files/teams/Student-Accommodation-Policy.pdf

Students needing an accommodation because of a disability or medical condition should communicate this need to Student Accessibility Services in accordance with the Procedure for Accommodations for Students with Disabilities: www.ucalgary.ca/legal-services/sites/default/files/teams/1/Policies-Accommodation-for-Students-with-Disabilities-Procedure.pdf

Students needing an accommodation in relation to their coursework or to fulfil requirements for a graduate degree, based on a protected ground other than disability, should communicate this need, preferably in writing, to their instructor.

13.2 Absence or missed course assessments

Students who are absent from class assessments (tests, participation activities, or other assignments) should inform their instructors as soon as possible. If the reason provided for the absence is acceptable, instructors may decide that any arrangements made can take forms other than make-up tests or assignments. For example, the weight of a missed grade may be added to another assignment or test.

13.3 Student support and resources

Full details and information about the following resources can be found at www.ucalgary.ca/current-students/student-services:

- Wellness and Mental Health Resources
- Student Success Centre
- Student Ombuds Office
- Student Union (SU) Information
- Graduate Students' Association (GSA) Information
- Emergency Evacuation/Assembly Points
- Safewalk

13.4 Academic Advising

If you are a student in the Faculty of Arts, you can speak to an academic advisor in the Arts Students' Centre about course planning, course selection, registration, program progression and more. Visit the Faculty of Arts website at arts.ucalgary.ca/current-students/undergraduate/academic-advising for contact details and information regarding common academic concerns.

For questions specific to the philosophy program, please visit arts.ucalgary.ca/philosophy. Further academic guidance is available by contacting Jeremy Fantl (Undergraduate Program Director, Email: jfantl@ucalgary.ca) or David Dick (Honours Advisor, Email: dgdick@ucalgary.ca). If you have questions regarding registration, please email Courtenay Canivet (Undergraduate Program Administrator, Email: phildept@ucalgary.ca).

13.5 Writing assessment and support

The assessment of all written assignments—and, to a lesser extent, written exam responses—is based in part on writing skills. This includes correctness (grammar, punctuation, sentence structure, etc.), as well as general clarity and organization. Research papers must include a thorough and accurate citation of sources. Students are also encouraged to use Writing Support Services for assistance (one-on-one appointments, drop-in support and writing workshops). For more information, and other services offered by the Student Success Centre, please visit ucalgary.ca/student-services/student-success.

13.6 Required technology

In order to successfully engage in their learning experiences at the University of Calgary, students taking online, remote and blended courses are required to have reliable access to the following technology:

- A computer with a supported operating system, as well as the latest security, and malware updates;
- A current and updated web browser;
- Webcam (built-in or external);
- Microphone and speaker (built-in or external), or headset with microphone;
- Current antivirus and/or firewall software enabled;
- Broadband internet connection.

Most current laptops will have a built-in webcam, speaker and microphone.

13.7 Responsible Use of D2L

Important information and communication about this course may be posted on D2L (Desire2Learn), UCalgary's online learning management system. Visit ucalgary.service-now.com/it for how-to information and technical assistance.

All users of D2L are bound by the guidelines on the responsible use of D2L posted at elearn.ucalgary.ca/commitment-to-the-responsible-use-of-d2l/. The instructor may establish additional specific course policies for D2L, Zoom, and any other technologies used to support remote learning. Instructional materials, including audio or video recordings of lectures, may not be posted outside of the course D2L site. Students violating this policy are subject to discipline under the University of Calgary's Non-Academic Misconduct policy, www.ucalgary.ca/legal-services/sites/default/files/teams/1/Policies-Student-Non-Academic-Misconduct-Policy.pdf

13.8 Media recording

Please refer to the following statement on media recording of students: elearn.ucalgary.ca/wp-content/uploads/2020/05/Media-Recording-in-Learning-Environments-OSP_FINAL.pdf.

13.9 Academic misconduct/honesty

Cheating or plagiarism on any assignment or examination is as an extremely serious academic offense, the penalty for which will be an F on the assignment or an F in the course, and possibly a disciplinary sanction such as probation, suspension, or expulsion. For information on academic misconduct and its consequences, please see the University of Calgary Calendar at: ucalgary.ca/pubs/calendar/current/k.html

Intellectual honesty requires that your work include adequate referencing to sources. Plagiarism occurs when you do not acknowledge or correctly reference your sources. If you have questions about referencing, please consult your instructor.

13.10 University policies

The Instructor Intellectual Property Policy is available at: www.ucalgary.ca/legal-services/sites/default/files/teams/1/Pol-Intellectual-Property-Policy.pdf

Course materials created by professor(s) (including course outlines, presentations, assignments, and exams) remain the intellectual property of the professor(s). These materials may *not* be reproduced, redistributed or copied without the explicit consent of the professor. The posting of course materials to third party websites such as note-sharing sites without permission is prohibited. Sharing of extracts of these course materials with other students enrolled in the course at the same time may be allowed under fair dealing.

The University of Calgary is under the jurisdiction of the provincial Freedom of Information and Protection of Privacy (FOIP) Act, as outlined at www.ucalgary.ca/legal-services/access-information-privacy. The instructor (or TA) must return graded assignments *directly* to the student **unless** written permission to do otherwise has been provided.

All students are required to read the University of Calgary policy on Acceptable Use of Material Protected by Copyright (www.ucalgary.ca/legal-services/sites/default/files/teams/1/Policies-Acceptable-Use-of-Material-Protected-by-Copyright-Policy.pdf) and requirements of the copyright act (laws-lois.justice.gc.ca/eng/acts/C-42/index.html).